

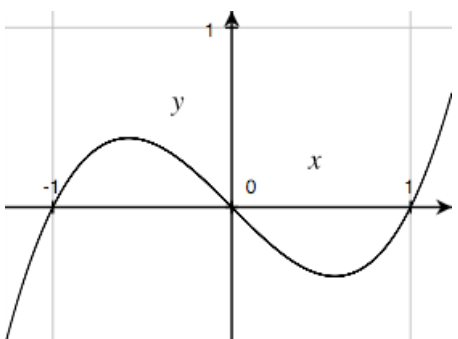
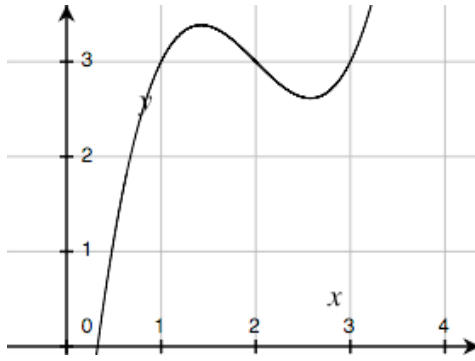
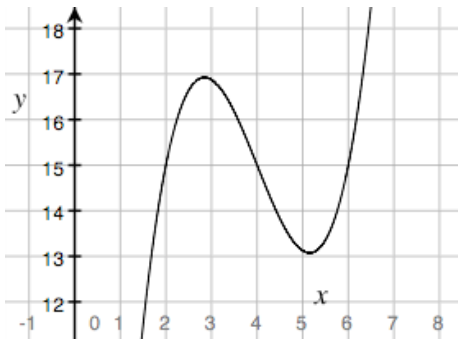
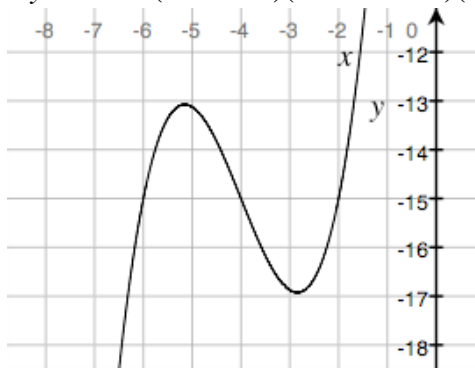
Essence of Basic Transformations

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Note: v represents one variable. In two dimensions, v could be x or y .

To	Replace v -values in all points by	Replace all parent relation's v -variables by
translate c units in v direction	$v + c$	$v - c$
dilate by c in v direction	cv	v/c ; $0 < c < 1$ shrinks, $1 < c$ stretches*
reflect in $v = 0$	$-v$	$-v$
reflect in origin	reflect in $v = 0$ for all v	
reflect in $y = x$	$(x, y) \rightarrow (y, x)$ in relation and all points. (Do this to get inverses. E.g., $y = e^x \rightarrow x = e^y \Leftrightarrow y = \ln x$.)	
rotate $+90^\circ$	$(x, y) \rightarrow (-y, x)$ in relation and all points. (If m is slope, then for lines: $l_1 \perp l_2 \Leftrightarrow m_2 = -1/m_1$)	

Examples:

<p>1. Parent, $y = x(x+1)(x-1)$:</p> 	<p>2. Translate up 3, right 2 (translation vector: $\langle 2, 3 \rangle$), $y - 3 = (x - 2)(x - 2 + 1)(x - 2 - 1)$:</p> 
<p>3. Stretch vertically 5 units and horizontally 2, $y/5 - 3 = (x/2 - 2)(x/2 - 2 + 1)(x/2 - 2 - 1)$</p> 	<p>4. Reflect in origin (note axes scales): $-y/5 - 3 = (-x/2 - 2)(-x/2 - 2 + 1)(-x/2 - 2 - 1)$</p> 

* Some texts treat stretching in x and y directions differently. In Blitzer, Precalculus, 2nd Ed, $y = f(x) \rightarrow y = c_y f(c_x x)$, where in the x direction $0 < c_x < 1$ stretches and $1 < c_x$ shrinks.